

Problems 1 chapter 8

①

$$\begin{aligned} \left[\frac{1}{2} I \omega^2 \right] &= [I] [\omega^2] \\ &= [\text{kg} \cdot \text{m}^2] [\text{rad/s}]^2 = [\text{kg} \cdot \text{m}^2/\text{s}^2] \\ &= \underbrace{[\text{kg} \cdot \text{m}^2/\text{s}^2]}_N \cdot [\text{m}] = [\text{N} \cdot \text{m}] = [\text{Joules}] \end{aligned}$$

⑤

a) Mass :  $\Rightarrow M = \rho V = \rho \frac{4}{3} \pi R^3$
density = ρ

$$\text{Thus } \frac{M_{\text{child}}}{M_{\text{adult}}} = \frac{\cancel{\rho} \frac{4}{3} \pi R_{\text{child}}^3}{\cancel{\rho} \frac{4}{3} \pi R_{\text{adult}}^3} = \left(\frac{R_{\text{child}}}{R_{\text{adult}}} \right)^3 = \left(\frac{1}{2} \right)^3 = \boxed{\frac{1}{8}}$$

$$\text{b) } I = \frac{2}{5} M R^2 \Rightarrow \frac{I_{\text{child}}}{I_{\text{adult}}} = \frac{\cancel{\frac{2}{5}} M_{\text{child}} R_{\text{child}}^2}{\cancel{\frac{2}{5}} M_{\text{adult}} R_{\text{adult}}^2}$$

$$\begin{aligned} &= \frac{M_{\text{child}}}{M_{\text{adult}}} \cdot \frac{R_{\text{child}}^2}{R_{\text{adult}}^2} \\ &= \left(\frac{1}{8} \right) \left(\frac{1}{2} \right)^2 = \boxed{\frac{1}{32}} \end{aligned}$$

⑨ A significant fraction of wheel's KE is rotational.

a) So it is NOT justified to model the wheel as if it were sliding without friction.

$$b) \frac{K_{\text{rotational}}}{K_{\text{total}}} = \frac{4\left(\frac{1}{2}I\omega^2\right)}{\frac{1}{2}Mv^2 + 4\left(\frac{1}{2}I\omega^2\right)}$$

Divide numerator and the denominator by $\frac{1}{2}I\omega^2 \Rightarrow$

$$\frac{K_{\text{rotational}}}{K_{\text{total}}} = \frac{4}{\frac{Mv^2}{I\omega^2} + 4}$$

but $\omega = \frac{v}{r}$; ($r = \text{radius of the wheel}$)

$$\frac{Mv^2}{I\omega^2} = \frac{Mr^2\cancel{\omega^2}}{I\cancel{\omega^2}} = \frac{Mr^2}{I} = \frac{(1300)(0.35)^2}{0.705} \approx 226$$

$$= \frac{4}{226 + 4} = \frac{4}{230} = \boxed{0.017}$$

In this case, 1.7% of K_{total} is rotational KE.

(13)

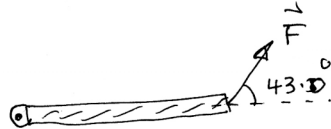
a)



$$\tau = r F_{\perp} = r F \sin \theta = r F \sin 90^\circ$$

$$\tau = (1.26)(46.4) = \boxed{58.5 \text{ N}\cdot\text{m}}$$

b)



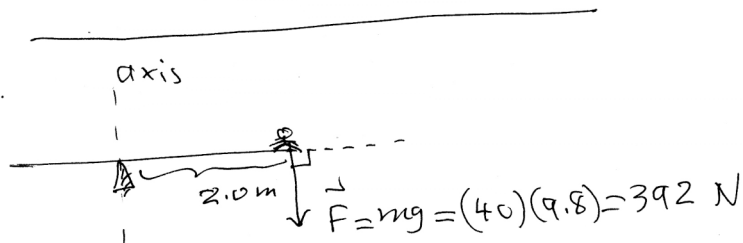
$$\tau = r F \sin \theta = (1.26)(46.4) \sin 43^\circ = \boxed{39.9 \text{ N}\cdot\text{m}}$$

c)



$$\tau = r F \sin \theta = (1.26)(46.4) \sin 0^\circ = \boxed{0}$$

(17)



$$\tau = r F \sin \theta = (2)(392)(\sin 90^\circ) = \boxed{784 \text{ N}\cdot\text{m}}$$

(25)

a) $\tau = I\alpha$

We need I and α ; $I = mR^2 = (182)(0.62)^2 = 70 \text{ kg}\cdot\text{m}^2$

for α , we use $w_f = w_i + \alpha \Delta t$

$$\left(120 \text{ rpm} \times \frac{2\pi}{60 \text{ s}}\right) = \alpha (30 \text{ s}) \Rightarrow \alpha = 0.42 \text{ rad/s}^2$$

$$\tau = I\alpha = (70)(0.42) = \boxed{29.3 \text{ N}\cdot\text{m}}$$

b) Work = ? $W = \tau\theta$

So we need θ : $\theta = w_i \Delta t + \frac{1}{2} \alpha \Delta t^2$

$$\theta = \left(\frac{1}{2}\right)(0.42)(30)^2 = 189 \text{ rad}$$

$$W = \text{work} = (29.3)(189) = \boxed{5538 \text{ J} \approx 5.5 \text{ kJ}}$$

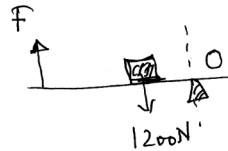
(31)

System in equilibrium

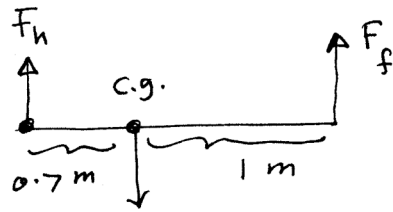
$\sum \tau = 0$. With respect

to Point O, $\sum \tau =$

$$\left(\sum \tau\right)_O = F(3.0) - (1200)(0.5) = 0 \Rightarrow$$
$$\boxed{F = 200 \text{ N}}$$



39



$$mg = (68 \times 9.8) = 666.4\text{ N}$$

$$\sum \vec{F} = 0 \Rightarrow F_h + F_f - 666.4 = 0 \Rightarrow F_h + F_f = 666.4 \quad (1)$$

$$\sum \tau = 0 : \text{choose pivot at } F_h \Rightarrow$$

$$(666.4)(0.7) - F_f(1 + 0.7) = 0 \Rightarrow F_f = 274.4\text{ N}$$

$$\text{Using Eq. (1)} \Rightarrow F_h = 392\text{ N}$$

53

$$\tau = I\alpha \quad \text{We need } I$$

$$I = \sum m_i r_i^2 = m_A r_A^2 + m_B r_B^2 + m_C r_C^2 + m_D r_D^2$$

$$\text{but } r_A = r_B = r_C = r_D = \frac{0.75}{2} = 0.375\text{ m}$$

$$\Rightarrow I = \dots = 1.97\text{ kg}\cdot\text{m}^2$$

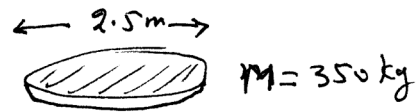
$$\text{Thus } \tau = I\alpha$$

$$\tau = (1.97)(0.75 \frac{\text{rad}}{\text{s}^2})$$

$$= 1.48\text{ N}\cdot\text{m}$$

55

$$m_{\text{child}} = 30 \text{ kg}$$



$$a) \tau = I \alpha$$

We need I and α .

$$\text{for calculating } \alpha : \quad \omega_f = \omega_i + \alpha \Delta t$$

$$\downarrow$$
$$\left(25 \times \frac{2\pi}{60} \right) = \alpha (20) \Rightarrow$$

$$\alpha = 0.13 \text{ rad/s}^2$$

$$\text{for calculating } I : \quad I = I_{\text{disk}} + I_{\text{children}}$$

$$I = \frac{MR^2}{2} + mR^2 + mR^2$$

$$= (350) \left(\frac{2.5}{2} \right)^2 + (30) \left(\frac{2.5}{2} \right)^2 + 30 \left(\frac{2.5}{2} \right)^2$$

$$I = 367.2 \text{ kg} \cdot \text{m}^2$$

$$\tau = (367.2) (0.13) \Rightarrow$$

$$\tau = 48 \text{ N} \cdot \text{m}$$

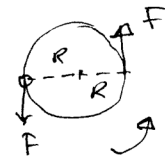
b)

$$\tau = FR + FR$$

$\downarrow$

$$48 = 2FR \Rightarrow$$

$$F = \frac{48}{2.5} = 19 \text{ N}$$



(62) a) $K_{\text{total}} = \frac{1}{2}mv^2 + \frac{1}{2}I\omega^2$
 $= \frac{1}{2}mv^2 + \frac{1}{2}(2/5 mR^2)\omega^2$
 Using $v = R\omega \Rightarrow K_{\text{total}} = \frac{7}{10}mv^2 = \boxed{10.5 \text{ J}}$

b) $\cancel{K_i} + U_i = K_f + \cancel{U_f}$
 $\downarrow$
 $mg y_i = K_f \Rightarrow y_i = \frac{10.5 \text{ J}}{(0.6)(9.8)} = \boxed{1.79 \text{ m}}$

(75) $L_i = 6.4 \text{ kg}\cdot\text{m}^2/\text{s}$ and $L_f = 0$ (to stop it)

$$\tau = \frac{\Delta L}{\Delta t} \Rightarrow 4 = \frac{6.4 - 0}{\Delta t}$$

$$\boxed{\Delta t = 1.6 \text{ s}}$$

Also check questions (78) and (79) to learn more about angular momentum.