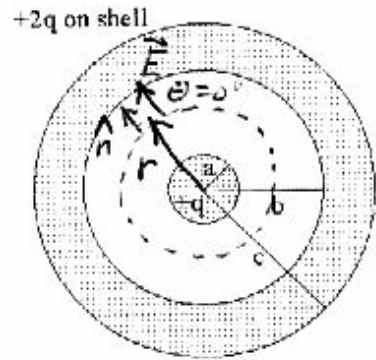


Name: KEY

PHYSICS 2220 - QUIZ #2 - SPRING 2009

1. A sphere, of radius a and charge $+q$ uniformly distributed throughout its volume, is concentric with a spherical conducting shell of inner radius b and outer radius c . This shell has a net charge of $+2q$.



- a. Find an expression for the electric field, as a function of the radius r , between the sphere and the shell ($a < r < b$).

$$\oint E dA \cos \theta = \frac{q_{enc}}{\epsilon_0} \quad \text{where } q_{enc} = +q$$

$$\oint E dA = \frac{q}{\epsilon_0} \quad \text{since } \cos 0^\circ = 1$$

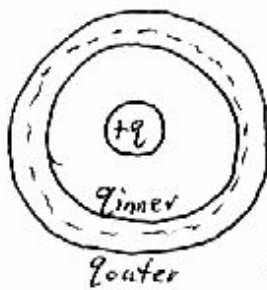
$$E \oint dA = \frac{q}{\epsilon_0} \quad \text{since } E = \text{constant over the gaussian sphere}$$

$$E 4\pi r^2 = \frac{q}{\epsilon_0}$$

$$E = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2}$$

- b. What are the charges on the inner and outer surfaces of the shell?

Draw a gaussian sphere between $r=b$ and $r=c$, where $E=0$



$$\oint E dA \cos \theta = \frac{q_{enc}}{\epsilon_0}$$

$$\text{Since } E=0, \quad q_{enc} = 0$$

$$\text{So } q_{enc} = +q + q_{inner} = 0 \Rightarrow q_{inner} = -q$$

$$\text{Since } q_{inner} + q_{outer} = +2q, \quad -q + q_{outer} = 2q$$

$$\Rightarrow q_{outer} = +3q$$