

MCQ 9

Solutions

Question 1

Use flow rate: $A_1 v_1 = A_2 v_2 \Rightarrow v_2 = \frac{A_1}{A_2} v_1$

(A) Thus $v_2 = \frac{\pi (2.5)^2}{\pi (1.5)^2} (0.54) = \boxed{1.5 \text{ m/s}}$

Question 2

Use Bernoulli's equation with $y_1 - y_2 = 4.5 \text{ m}$

a) $P_1 + \frac{1}{2} \rho v_1^2 + \rho g y_1 = P_2 + \frac{1}{2} \rho v_2^2 + \rho g y_2$

but $P_1 = P_2$ and $v_1 = 0$ (see example 9.10)

$\Rightarrow \cancel{\rho} g y_1 = \frac{1}{2} \cancel{\rho} v_2^2 + \cancel{\rho} g y_2 \Rightarrow \boxed{v_2 = 9.4 \text{ m/s}}$

(A)

b) Use flow rate $= Av$

↓

Volume $\leftarrow \frac{\Delta V}{\text{time} \leftarrow \Delta t} = Av \Rightarrow \Delta V = \Delta t \times A \times v$

$\downarrow \quad \quad \downarrow \quad \quad \downarrow$
 $(60 \text{ s}) \quad (0.25 \times 10^{-4}) \quad (9.4)$

$\boxed{\Delta V = 0.014 \text{ m}^3}$

Question 3

$$P_1 + \frac{1}{2} \rho v_1^2 + \rho g y_1 = P_2 + \frac{1}{2} \rho v_2^2 + \rho g y_2$$

but $y_1 - y_2 = 4 \text{ m}$, $\rho = 1000 \text{ kg/m}^3$, we need v_1 and v_2

Since flow rate is given $= 0.08 \text{ m}^3/\text{s}$ we can solve

for v_1 and v_2 :

$$\text{flow rate} = A v \Rightarrow 0.08 = A_1 v_1 \rightarrow v_1 = \frac{0.08}{\pi(0.1)^2}$$

$$v_1 = 2.55 \text{ m/s}$$

$$\text{Also: } 0.08 = A_2 v_2 \rightarrow v_2 = \frac{0.08}{\pi(0.15)^2} = 1.13 \text{ m/s}$$

Thus:

$$\rightarrow 130 \times 10^3 + \frac{1}{2} (1000) (2.55)^2 + 1000 \times 9.8 \times y_1 =$$

(A)

$$P_2 + \frac{1}{2} (1000) (1.13)^2 + 1000 \times 9.8 \times y_2$$

using $y_2 - y_1 = 4 \text{ m} \Rightarrow$ Solve for P_2

$$P_2 = 93 \times 10^3 \text{ Pa}$$

Question 4: $P = 4 \times 10^5 \text{ Pa}$

(D)

$$P = \frac{F}{A} \Rightarrow F = PA = \dots = 4000 \text{ N}$$

Question 5

(B)

$$P_{\text{liquid}} = \rho g d$$

$$= 1000 \times 9.8 \times 26 = \boxed{255 \text{ kPa}}$$

Question 6

$$\Delta P = 760 - 210 = 550 \text{ mm Hg}$$

$$\downarrow \text{ in pascal } \Delta P = \frac{550}{760} \times 1.013 \times 10^5 = 73.3 \text{ kPa}$$

This is one atm

(D)

$$F = (\Delta P) A = (73.3 \times 10^3 \text{ Pa}) (600 \times 10^{-4} \text{ m}^2)$$

$$= \boxed{4400 \text{ N}}$$

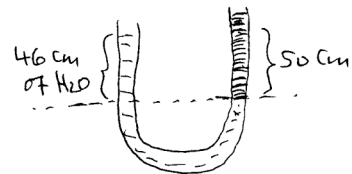
Question 7

At the dashed line:

$$P_{\text{left}} = P_{\text{right}}$$

$$\rho_{\text{H}_2\text{O}} g d_{\text{H}_2\text{O}} = \rho_{\text{oil}} g d_{\text{oil}}$$

$$\downarrow (1000)(0.46) = (\rho_{\text{oil}})(0.5) \Rightarrow \boxed{\rho_{\text{oil}} = 920 \text{ kg/m}^3}$$



(A)

Question 8

$$P_{\text{atm}} = 1.0 \times 10^5 \text{ Pa}$$

$$P_{\text{oil}} = \rho_{\text{oil}} g d_{\text{oil}} = (0.78 \times 10^3 \text{ kg/m}^3)(9.8)(0.27)$$

(A)

$$P_{\text{oil}} = 2064 \text{ Pa}$$

$$P_{\text{chamber}} = 1.0 \times 10^5 - 2064 \approx 98 \times 10^3 \text{ Pa}$$

Question 9

$$W_{\text{apparent}} = W_{\text{cube}} - F_B$$
$$\downarrow \qquad \qquad \qquad \downarrow$$
$$(P_{\text{cube}} \times V_{\text{cube}} \times g) - (P_{\text{H}_2\text{O}} \times V_{\text{cube}} \times g)$$

(D)

$$\text{where } V_{\text{cube}} = (0.02)^3$$

$$W_{\text{apparent}} = \dots = 0.43 \text{ N}$$

$$\downarrow$$
$$m_{\text{apparent}} = \frac{0.43}{9.8} = 0.0448 \text{ kg}$$
$$= 44.8 \text{ g}$$

Question 10

$$\text{Tension} = W_{\text{apparent}} \quad (\text{apparent weight in oil})$$

$$\Rightarrow W_{\text{apparent}} = W_{\text{Al}} - F_B = \left(\frac{8.35}{1000} \text{ kg}\right)(9.8) - \rho_{\text{oil}} V_{\text{Al}} g$$

(A)

$$\text{We need } V_{\text{Al}} = \frac{0.00835 \text{ kg}}{2700 \text{ kg/m}^3} = 3 \times 10^{-6} \text{ m}^3 \quad \left(0.75 \times 10^3 \text{ kg/m}^3\right)$$

$$\text{Thus } W_{\text{apparent}} = \text{Tension} = 0.059 \text{ N}$$